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signed char has range -128 to 127 and the unsigned char has range 0 to 255, so the intersection type of these two types would be range 0 to 127. Such a function could be safely passed into functions expecting either signed or unsigned chars, because it is compatible with both types. Intersection types are useful for describing overloaded function types: for example, if `int → int` is the type of functions taking an integer argument and returning an integer, and `float → float` is the type of functions taking a float argument and returning a float, then the intersection of these two types can be used to describe functions that do one or the other, based on what type of input they are given. Such a function could be passed into another function expecting an `int → int` function safely; it simply would not use the `float → float` functionality. In a subclassing hierarchy, the intersection of a type and an ancestor type (such as its parent) is the most derived type. The intersection of sibling types is empty. The Forsythe language includes a general implementation of intersection types. A restricted form is refinement types. Main article: Union type
Union types are types describing values that belong to either of two types. For example, in C, the signed char has a -128 to 127 range, and the unsigned char has a 0 to 255 range, so the union of these two types would have an overall "virtual" range of -128 to 255 that may be used partially depending on which union member is accessed. Any function handling this union type would have to deal with integers in this complete range. More generally, the only valid operations on a union type are operations that are valid on both types being unioned. C's "union" concept is similar to union types, but is not typesafe, as it permits operations that are valid on either type, rather than both. Union types are important in program analysis, where they are used to represent symbolic values whose exact nature (e.g., value or type) is not known. In a subclassing hierarchy, the union of a type and an ancestor type (such as its parent) is the ancestor type. The union of sibling types is a subtype of their common ancestor (that is, all operations permitted on their common ancestor are permitted on the union type, but they may also have other valid operations in common). Main article: Existential quantifier
Existential types are frequently used in connection with record types to represent modules and abstract data types, due to their ability to separate implementation from interface. For example, the type `T = ∃X { a: X; f: (X → int); }` describes a module interface that has a data member named `a` of type `X` and a function named `f` that takes a parameter of the same type `X` and returns an integer. This could be implemented in different ways; for example: `intT = { a: int; f: (int → int); }` `floatT = { a: float; f: (float → int); }` These types are both subtypes of the more general existential type `T` and correspond to concrete implementation types, so any value of one of these types is a value of type `T`. Given a value `t` of type `T`, we know that `Lift(t)` is well-typed, regardless of what the abstract type `X` is. This gives flexibility for choosing types suited to a particular implementation, while clients that use only values of the interface type—the existential type—are isolated from these choices. In general it's impossible for the typechecker to infer which existential type a given module belongs to. In the above example `intT { a: int; f: (int → int); }` could also have the type `∃X { a: X; f: (int → int); }`. The simplest solution is to annotate every module with its intended type, e.g.: `intT = { a: int; f: (int → int); }` as `∃X { a: X; f: (X → int); }` Although abstract data types and modules had been implemented in programming languages for quite some time, it wasn't until 1988 that John C. Mitchell and Gordon Plotkin established the formal theory under the slogan: "Abstract [data] types have existential type".[25] The theory is a second-order typed lambda calculus similar to System F, but with existential instead of universal quantification. Main article: Gradual typing
In a type system with Gradual typing, variables may be assigned a type either at compile-time (which is static typing), or at run-time (which is dynamic typing).[26] This allows software developers to choose either type paradigm as appropriate, from within a single language.[26] Gradual typing uses a special type named *dynamic* to represent statically unknown types; gradual typing replaces the notion of type equality with a new relation called *consistency* that relates the dynamic type to every other type. The consistency relation is symmetric but not transitive.[27] Further information: Type inference
Many static type systems, such as those of C and Java, require type declarations: the programmer must explicitly associate each variable with a specific type. Others, such as Haskell's, perform type inference: the compiler draws conclusions about the types of variables based on how programmers use those variables. For example, given a function `f(x, y)` that adds `x` and `y` together, the compiler can infer that `x` and `y` must be numbers—since addition is only defined for numbers. Thus, any call to `f` elsewhere in the program that specifies a non-numeric type (such as a string or list) as an argument would signal an error. Numerical and string constants and expressions in code can and often do imply type in a particular context. For example, an expression `3.14` might imply a type of floating-point, while `[1, 2, 3]` might imply a list of integers—typically an array. Type inference is in general possible, if it is computable in the type system in question. Moreover, even if inference is not computable in general for a given type system, inference is often possible for a large subset of real-world programs. Haskell's type system, a version of Hindley–Milner, is a restriction of System F_ω to so-called rank-1 polymorphic types, in which type inference is computable. Most Haskell compilers allow arbitrary-rank polymorphism as an extension, but this makes type inference not computable. (Type checking is decidable, however, and rank-1 programs still have type inference; higher rank polymorphic programs are rejected unless given explicit type annotations.) Main article: Type theory
§ Decision problems
A type system that assigns types to terms in type environments using typing rules is naturally associated with the decision problems of type checking, typability, and type inhabitation.[28] Given a type environment

Γ

{\displaystyle \Gamma }

, a term

e

{\displaystyle e}

, and a type

τ

{\displaystyle \tau }

, decide whether the term

e

{\displaystyle e}

 can be assigned the type

τ

{\displaystyle \tau }

 in the type environment. Given a term

e

{\displaystyle e}

, decide whether there exists a type environment

Γ

{\displaystyle \Gamma }

 such that the term

e

{\displaystyle e}

 can be assigned the type

τ

{\displaystyle \tau }

 in the type environment

Γ

{\displaystyle \Gamma }

. Given a type environment

Γ

{\displaystyle \Gamma }

 and a type

τ

{\displaystyle \tau }

, decide whether there exists a term

e

{\displaystyle e}

 that can be assigned the type

τ

{\displaystyle \tau }

 in the type environment. Some languages like C# or Scala have a unified type system.[29] This means that all C# types including primitive types inherit from a single root object. Every type in C# inherits from the Object class. Some languages, like Java and Raku, have a root type but also have primitive types that are not objects.[30] Java provides wrapper object types that exist together with the primitive types so developers can use either the wrapper object types or the simpler non-object primitive types. Raku automatically converts primitive types to objects when their methods are accessed.[31]
A type checker for a statically typed language must verify that the type of any expression is consistent with the type expected by the context in which that expression appears. For example, in an assignment statement of the form `x = e`, the inferred type of the expression `e` must be consistent with the declared or inferred type of the variable `x`. This notion of consistency, called *compatibility*, is specific to each programming language. If the type of `e` and the type of `x` are the same, and assignment is allowed for that type, then this is a valid expression. Thus, in the simplest type systems, the question of whether two types are compatible reduces to that of whether they are equal (or equivalent). Different languages, however, have different criteria for when two type expressions are understood to denote the same type. These different equational theories of types vary widely, two extreme cases being structural type systems, in which any two types that describe values with the same structure are equivalent, and nominative type systems, in which no two syntactically distinct type expressions denote the same type (i.e., types must have the same "name" in order to be equal). In languages with subtyping, the compatibility relation is more complex: If B is a subtype of A, then a value of type B can be used in a context where one of type A is expected (covariant), even if the reverse is not true. Like equivalence, the subtype relation is defined differently for each programming language, with many variations possible. The presence of parametric or ad hoc polymorphism in a language may also have implications for type compatibility.
Computer programming portal
Comparison of type systems
Covariance and contravariance (computer science)
Polymorphism in object-oriented programming
Type signature
Type theory
^ The Burroughs ALGOL computer line determined a memory location's contents by its flag bits. Flag bits specify the contents of a memory location. Instruction, data type, and functions are specified by a 3 bit code in addition to its 48 bit contents. Only the MCP (Master Control Program) could write to the flag code bits.
^ For example, a leaky abstraction might surface during development, which may show that more type development is needed.
—"The evaluation of a well-typed program always terminates"—B. Nordström, K. Petersson, and J. M. Smith[5]
A systematic change in variables to avoid capture of a free variable can introduce error, in a functional programming language where functions are first class citizens.[6]
—From the lambda calculus article.
^ Pierce 2002, p. 1; "A type system is a tractable syntactic method for proving the absence of certain program behaviors by classifying phrases according to the kinds of values they compute."
^ Cardelli 2004, p. 1; "The fundamental purpose of a type system is to prevent the occurrence of execution errors during the running of a program."
^ Pierce 2002, p. 208.
^ a b Sethi, R. (1996). Programming languages: Concepts and constructs (2nd ed.). Addison-Wesley. p. 142. ISBN 978-0-201-59065-4. OCLC 604732680.
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^ "... any sound, decidable type system must be incomplete" —D. Remy (2017), p. 29, Remy, Didier. "Type systems for programming languages" (PDF). Archived from the original (PDF) on 14 November 2017. Retrieved 26 May 2013.
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